

Supporting information

SI #1. Estimation of boundary layer thickness and time for boundary layer development

From laminar boundary layer theory,¹ using an average mass transfer coefficient of 0.023 cm/min obtained from the fitting procedure, we can construct the following correlation for the mass transfer coefficient:

$$k_m = 7.03 \left(\frac{D^2 Q}{h^2 d^2} \right)^{\frac{1}{3}}. \quad (S1)$$

Here, $h = 640 \mu\text{m}$ and $d = 1.1 \text{ cm}$ are the depth and diameter, respectively, of the QCM-D device, D is the diffusivity of MBP equal to $3.5 \times 10^{-11} \text{ m}^2/\text{s}$,² and $Q = 400 \mu\text{l/s}$ is the volumetric flow rate through the QCM-D chamber. The approximate concentration boundary layer thickness, δ_m , is¹

$$\delta_m \sim \frac{D}{k_m} = 0.142 \left(\frac{h^2 d^2 D}{Q} \right)^{\frac{1}{3}}. \quad (S2)$$

For the parameters above, the boundary thickness is about $9 \mu\text{m}$. The characteristic time for diffusion of MBP over $9 \mu\text{m}$ is $\delta_m^2 / D \approx 2.3$ seconds, which is extremely short compared to the kinetic time scales being examined in the QCM-D experiments.

SI #2. Non-dimensionalized equations with fitting parameters

Equations

Using $\underline{C}_C^* = \frac{C_C}{C_{ch}}$, $\underline{C}_D^* = \frac{C_D}{C_{ch}}$ and $\underline{t}^* = \frac{t}{t_{ch}}$, we get

$$\frac{d\underline{C}_C}{d\underline{t}} = \alpha\beta \left(\frac{\gamma\theta_f - \underline{C}_C}{\alpha + \theta_f} \right) - \delta\underline{C}_C. \quad (7')$$

$$\frac{d\underline{C}_D}{d\underline{t}} = \delta\underline{C}_C \quad (8')$$

$$\underline{C}_0 = \underline{C}_C + \underline{C}_D \quad (9')$$

$$\theta_f = 1 - \frac{C_{ch}}{C_{Csat}} \underline{C}_C - \frac{C_{ch}}{C_{Dsatsat}} \underline{C}_D \quad (3')$$

Fitting Parameters

$$\alpha = \frac{k_m}{k_1}$$

$$\beta = k_{-1}t_{ch}$$

$$\gamma = \frac{k_1 C_{A0}}{k_{-1} C_{ch}}$$

$$\delta = k_2 t_{ch}$$

SI #3. Raw QCM data

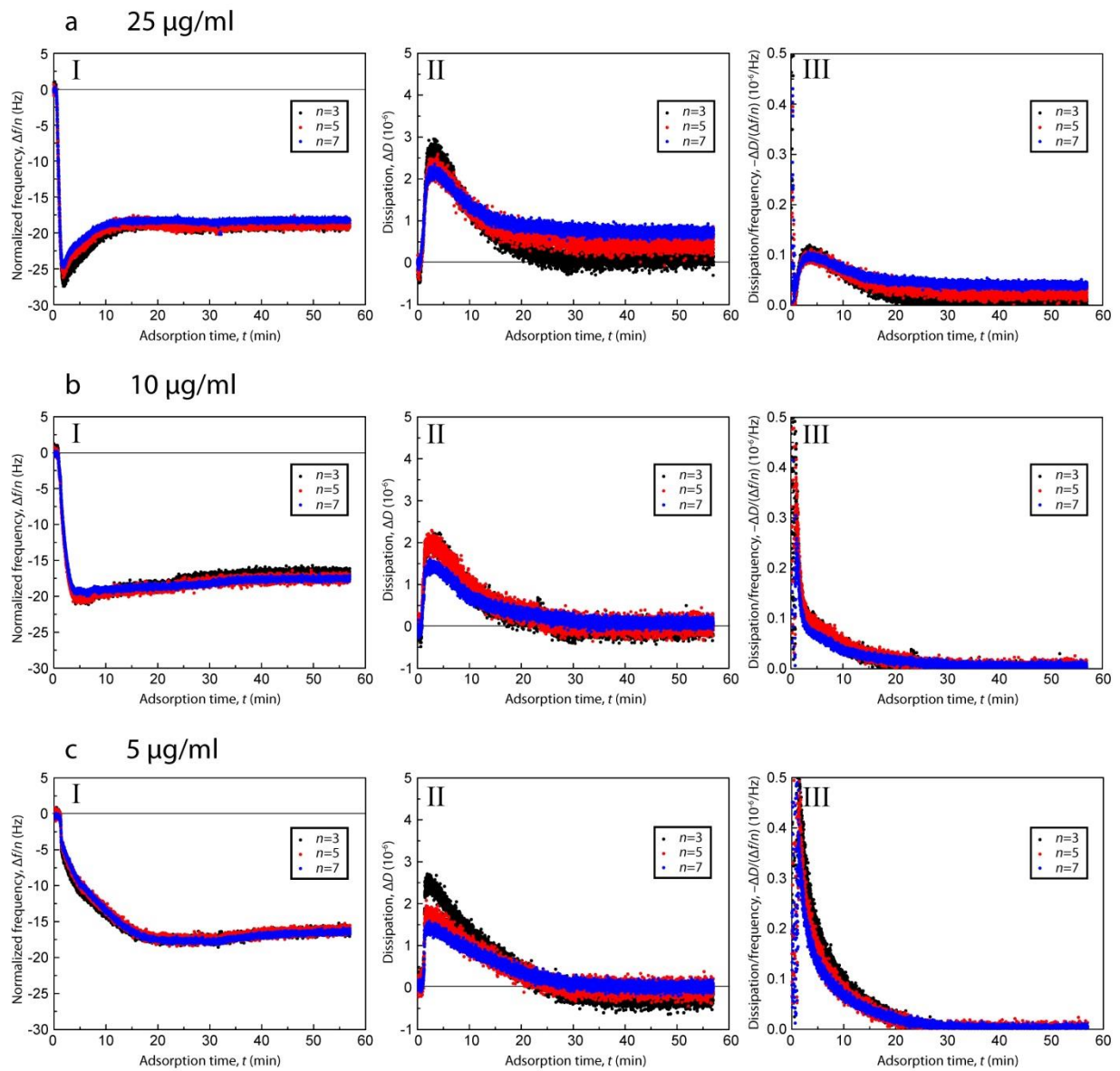


Figure S1. Series of raw QCM-D data at MBP concentrations of (a) 25 $\mu\text{g/ml}$, (b) 10 $\mu\text{g/ml}$, and (c) 5 $\mu\text{g/ml}$. (I) Normalized frequency shift, $\Delta f/n$, (II) Dissipation, ΔD , and (III) ratio between frequency and dissipation, $\Delta D/(\Delta f/n)$, have been shown. n indicates overtone numbers.

SI references

1. Leal, L. G., *Advanced Transport Phenomena: Fluid Mechanics and Convective Transport Processes*. Cambridge University Press: New York, 2007.
2. Stadler, A. M.; Stingaciu, L.; Radulescu, A.; Holderer, O.; Monkenbusch, M.; Biehl, R.; Richter, D., Internal Nanosecond Dynamics in the Intrinsically Disordered Myelin Basic Protein. *Journal of the American Chemical Society* **2014**, 136, (19), 6987-6994.